

Universality of Short-Range Correlations in One- and Two-Nucleon Momentum Distributions of Nuclei

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Abstract. Universality of short range correlations has been investigated both in coordinate and in momentum space, by means of one- and two-body densities and momentum distributions. In this contribution we discuss one- and two-body momentum distributions across a wide range of nuclei and their common features which can be ascribed to the presence of short range correlations. Calculations for few-body nuclei, namely ^3He and ^4He , have been performed using exact wave functions obtained with Argonne nucleon-nucleon interactions, while the linked cluster expansion technique is used for medium-heavy nuclei. The center of mass motion of a nucleon-nucleon pair in the nucleus, embedded in the full two-body momentum distribution $n^{NN}(\mathbf{k}_{rel}, \mathbf{K}_{CM})$, is shown to exhibit the universal behavior predicted by the two-nucleon correlation model, in which the nucleon-nucleon pair moves inside the nucleus as a deuteron in a mean-field. Moreover, the deuteron-like spin-isospin (ST)=(10) contribution to the pn two-body momentum distribution is obtained, and shown to exactly scale to the deuteron momentum distribution. Universality of correlations in two-body distributions is cast onto the one-body distribution $n(k_1)$, obtained by integration of the two-body $n^{NN}(\mathbf{k}_1, \mathbf{k}_2)$: in particular, the high momentum part of $n(k_1)$ exhibits the same pattern for all considered nuclei, in favor of a universal character of the short range structure of the nuclear wave function. Perspectives of this work, namely the calculation of reactions involving light and complex nuclei with realistic wave functions and effects of Final State Interactions (FSI), investigated by means of distorted momentum distributions within the Glauber multiple scattering approach, are eventually discussed.

We report on recent developments on the investigation of Short Range Correlations (SRC) in nuclei, whose common properties have recently been studied by a few authors in light [1–5] and medium-heavy [6–9] nuclei using realistic nuclear wave functions. Common properties among different nuclei have been investigated both in coordinate and momentum space using various methods and Nucleon-Nucleon (NN) interaction potentials for generating nuclear wave functions. Such an effort from the theoretical side was motivated by the recent observation of NN SRC in different experiments (reviewed in [10]): two

nucleon at high four-momentum transfer with protons and electrons, namely $A(p,ppN)X$ of Ref. [11] and $A(e,e'pN)X$ of Refs. [12,13], and inclusive electron scattering $A(e,e')X$ of Refs. [14,15], have provided evidence that NN SRC: i) exist in the ground-state wave function of nuclei; ii) can be detected in different reactions, using different projectiles and final states, suggesting some universal character, though direct measurement of two nucleons in a correlated pair have been performed only in the carbon nucleus; iii) are dominated by tensor correlations, which is suggested by the small observed fraction of correlated proton-proton pair as compared to the proton-neutron ones, and originating from the two-body tensor operator acting between pairs of nucleons in a state with spin $S=1$ and isospin $T=0$. Universality patterns observed in momentum space in the high-momentum region, correspond to similar behavior in coordinate space [4,16–19]. Moreover, the existence of SRC in nuclei has been related to nuclear EMC effect and poses the question of the validity of many of the proposed models of the EMC effect [20,21].

The dominance of the tensor part of the NN interaction and its effects on the two-body momentum distributions were clearly described from different theoretical groups for light [1] and medium-heavy nuclei [7,8]. Moreover, the pn vs. pp content of the two-body momentum distributions of a nucleon pair with zero center of mass was calculated in Ref. [7], and found to be compatible with the observed ratio of pn over pp correlated pairs. Nevertheless, a consistent and quantitative description of the detected pairs in the experimental kinematics should use the full information contained in the wave functions, so that the center of mass momentum of the pair is allowed to be different from zero, and should take into account the complex FSI suffered by the two nucleons before leaving the nucleus and being detected.

The calculation of the center of mass dependence of two-body momentum distributions for light [3] and medium-heavy nuclei [22,23] has been performed with exact wave functions [24,25], in the first case, while it relies on the linked cluster expansion method presented in Refs. [26,27], in the case of $A \geq 12$. The linked cluster expansion formalism makes use of variationally determined correlation functions coupled to the spin-isospin dependent operators adopted by realistic interactions. The correlation function approach is common to several methods, and it is used to describe both finite nuclei [28–32] and nuclear matter [33–38]. The linked cluster expansion method allows the computational demand to be reduced with respect to exact methods, so that the full one- and two-body, diagonal and non-diagonal density distributions can be calculated, along with the individual contributions of given spin and isospin states.

The distributions discussed in this contribution, for all the nuclei we considered, are obtained by computing the expectation value of suitable operators on the ground-state wave function. The non-diagonal one-body density is obtained

as:

$$\rho_N^{(1)}(\mathbf{r}_1; \mathbf{r}'_1) = \sum_{\{\sigma, \tau\}} \int \prod_{j=2}^A d\mathbf{r}_j d\mathbf{r}'_j \Psi^*(\{\mathbf{x}\}) \hat{\rho}^{(1)} \Psi(\{\mathbf{x}'\}), \quad (1)$$

while the two-body density is:

$$\rho_{NN}^{(2)}(\mathbf{r}_1, \mathbf{r}_2; \mathbf{r}'_1, \mathbf{r}'_2) = \sum_{\{\sigma, \tau\}} \int \prod_{j=3}^A d\mathbf{r}_j d\mathbf{r}'_j \Psi^*(\{\mathbf{x}\}) \hat{\rho}^{(2)} \Psi(\{\mathbf{x}'\}), \quad (2)$$

where $\{\sigma\}$ and $\{\tau\}$ stand for the spin and isospin degrees of freedom, respectively, of the A nucleons; $\mathbf{x} = \{\mathbf{r}, \sigma, \tau\}$, and the primed variables stands for fluctuation of the spatial part \mathbf{r} , while the spin and isospin variables of the corresponding particle are fixed. We use a Slater determinant Φ of shell model single particle wave function for Ψ , and the correlations are implemented, by means of an operator \hat{F} containing the correlation functions and corresponding state-dependent operators [27]: $\Psi(\mathbf{x}_1, \dots, \mathbf{x}_A) = \hat{F}(\mathbf{x}_1, \dots, \mathbf{x}_A) \Phi(\mathbf{x}_1, \dots, \mathbf{x}_A)$, in such a way that the final wave function is totally antisymmetric.

The operators appearing in Eqs. (1) and (2) are respectively defined as:

$$\hat{\rho}^{(1)} = \sum_i^A \delta(\mathbf{r}_i - \tilde{\mathbf{r}}_1) \delta(\mathbf{r}'_i - \tilde{\mathbf{r}}'_1) \prod_{k \neq i}^A \delta(\mathbf{r}_k - \mathbf{r}'_k); \quad (3)$$

$$\hat{\rho}^{(2)} = \sum_{i < j}^A \delta(\mathbf{r}_i - \tilde{\mathbf{r}}_1) \delta(\mathbf{r}_j - \tilde{\mathbf{r}}_2) \delta(\mathbf{r}'_i - \tilde{\mathbf{r}}'_1) \delta(\mathbf{r}'_j - \tilde{\mathbf{r}}'_2) \prod_{k \neq i, j}^A \delta(\mathbf{r}_k - \mathbf{r}'_k). \quad (4)$$

The one- and two-body momentum distributions are obtained from Eqs. (1) and (2) by proper Fourier transformations:

$$n^N(k_1) = \frac{1}{(2\pi)^3} \int d\mathbf{r}_1 d\mathbf{r}'_1 e^{i\mathbf{k}_1 \cdot (\mathbf{r}_1 - \mathbf{r}'_1)} \rho_N^{(1)}(\mathbf{r}_1; \mathbf{r}'_1), \quad (5)$$

$$n^{NN}(\mathbf{k}_1, \mathbf{k}_2) = \frac{1}{(2\pi)^6} \int d\mathbf{r}_1 d\mathbf{r}_2 d\mathbf{r}'_1 d\mathbf{r}'_2 e^{i\mathbf{k}_1 \cdot (\mathbf{r}_1 - \mathbf{r}'_1)} \cdot e^{i\mathbf{k}_2 \cdot (\mathbf{r}_2 - \mathbf{r}'_2)} \rho_{NN}^{(2)}(\mathbf{r}_1, \mathbf{r}_2; \mathbf{r}'_1, \mathbf{r}'_2); \quad (6)$$

the two-body momentum distributions can be conveniently rewritten in terms of the relative and center of mass momenta as follows:

$$n^{NN}(\mathbf{k}_{rel}, \mathbf{K}_{CM}) = \frac{1}{(2\pi)^6} \int d\mathbf{r} d\mathbf{R} d\mathbf{r}' d\mathbf{R}' e^{i\mathbf{k}_{rel} \cdot (\mathbf{r} - \mathbf{r}')} \cdot e^{i\mathbf{K}_{CM} \cdot (\mathbf{R} - \mathbf{R}')} \rho(\mathbf{r}, \mathbf{R}; \mathbf{r}', \mathbf{R}'), \quad (7)$$

were $\mathbf{r} = \mathbf{r}_1 - \mathbf{r}_2$, $\mathbf{R} = (\mathbf{r}_1 + \mathbf{r}_2)/2$ (and analogous definitions for the primed vectors) and $\mathbf{k}_{rel} = (\mathbf{k}_1 - \mathbf{k}_2)/2$, $\mathbf{K}_{CM} = \mathbf{k}_1 + \mathbf{k}_2$. The partial spin and isospin

contributions to the quantities above have been obtained by complementing the density operators of Eq. (4) by the projection operators on specific total spin S and isospin T of the “1,2” NN pair; extended definitions, normalization conditions and relations between the various formulas of Eqs. (1) and (2) are given in Ref. [6]. It is worth mentioning that actual calculations of two-body momentum distributions, which are obtained by sampling the one- and two-body densities after multidimensional integration of the few-body wave functions, in the case of ^3He and ^4He , and of the corresponding linked cluster expansion formulas given in details in Refs. [27, 39], for complex nuclei, are the following. In the case of the relative two-body distribution, obtained by integrating Eq. (7) over the center of mass momentum, we use the following coordinates: $\mathbf{x} = \mathbf{r} - \mathbf{r}'$, $\mathbf{t} = \frac{1}{2}(\mathbf{r} + \mathbf{r}')$, $\mathbf{s} = \mathbf{R} - \mathbf{R}'$ and $\mathbf{w} = \frac{1}{2}(\mathbf{R} + \mathbf{R}')$. Performing the coordinate transformation into Eq. (7) and integrating over K_{CM} , we have:

$$\begin{aligned}
 n_{rel}^{NN}(k_{rel}) &= \int d\mathbf{K}_{CM} n^{NN}(\mathbf{k}_{rel}, \mathbf{K}_{CM}) = \\
 &= \frac{1}{(2\pi)^3} \int d\mathbf{x} dt ds d\mathbf{w} e^{i\mathbf{k}_{rel}\cdot\mathbf{x}} \rho_{NN}^{(2)}(\mathbf{x}, \mathbf{t}, \mathbf{s}, \mathbf{w}) = \\
 &= \frac{1}{(2\pi)^3} \int d\mathbf{x} e^{i\mathbf{k}_{rel}\cdot\mathbf{x}} \rho_{NN}^{(2)}(x) = \\
 &= \frac{1}{2\pi^2} \int_0^\infty dx x \frac{\sin k_{rel} x}{k_{rel}} \rho_{NN}^{(2)}(x), \tag{8}
 \end{aligned}$$

where we choose \mathbf{k}_{rel} along a given direction that we define as the z axis and with, obviously:

$$\rho_{NN}^{(2)}(x) = \int dt ds d\mathbf{w} \rho_{NN}^{(2)}(\mathbf{x}, \mathbf{t}, \mathbf{s}, \mathbf{w}), \tag{9}$$

with $x = |\mathbf{x}|$. Analogously, we have

$$n_{CM}^{NN}(K_{CM}) = \frac{1}{2\pi^2} \int_0^\infty ds s \frac{\sin K_{CM} s}{K_{CM}} \rho_{NN}^{(2)}(s). \tag{10}$$

In the case we want to fix a few (*small*) values of \mathbf{K}_{CM} , and plot the resulting k_{rel} distribution, we have to choose the relative orientation of \mathbf{k}_{rel} and \mathbf{K}_{CM} . If we choose both of the them along the same direction, for example z , Eq. (7) becomes

$$\begin{aligned}
 n_{\parallel}^{NN}(\mathbf{k}_{rel}, K_{CM}) &= \\
 &= \frac{1}{(2\pi)^6} Re \int d\mathbf{x} dt ds d\mathbf{w} e^{i\mathbf{K}_{CM}\cdot\mathbf{s}} e^{i\mathbf{k}_{rel}\cdot\mathbf{x}} \rho_{NN}^{(2)}(\mathbf{x}, \mathbf{t}, \mathbf{s}, \mathbf{w}) = \\
 &= \frac{1}{(2\pi)^6} Re \int d\mathbf{x} dt ds d\mathbf{w} e^{iK_{CM} s_z} e^{i k_{rel} x_z} \rho_{NN}^{(2)}(\mathbf{x}, \mathbf{t}, \mathbf{s}, \mathbf{w}) = \\
 &= \frac{1}{(2\pi)^6} \int_{-\infty}^\infty dx_z ds_z \cos(k_{rel} x_z + K_{CM} s_z) \rho_{NN}^{(2)}(x_z, s_z), \tag{11}
 \end{aligned}$$

where, in this case, we have to sample a two-dimensional $\rho_{NN}^{(2)}(x_z, s_z)$, defined as

$$\rho_{NN}^{(2)}(x_z, s_z) = \int dt d\mathbf{w} dx_x dx_y ds_x ds_y \rho_{NN}^{(2)}(\mathbf{x}, \mathbf{t}, \mathbf{s}, \mathbf{w}), \quad (12)$$

and we have taken the real part in Eq. (11). Similarly, we can calculate the distribution in the case of the relative momentum perpendicular to the center of mass momentum:

$$n_{\perp}^{NN}(\mathbf{k}_{rel}, K_{CM}) = \int \frac{dx_z ds_x}{(2\pi)^6} \cos(k_{rel} x_z + K_{CM} s_x) \rho_{NN}^{(2)}(x_z, s_x), \quad (13)$$

with $\rho_{NN}^{(2)}(x_z, s_x)$ defined accordingly; in this case, we choose k_{rel} along the z axis, and K_{CM} along the x axis. Results for the parallel case, Eq. (11), are shown in Fig. 1, for various nuclei. We also compare these results with the predictions of the Two-Nucleon Correlation (TNC) model, where the relative distribution is taken as the deuteron's one, and the center of mass Gaussian distribution of the model has been replaced by actual values of $n_{CM}^{pn}(K_{CM})$, the two-body momentum distributions integrated over the relative momentum, Eq. (10).

The general conclusions that can be drawn about the two-body momentum distribution $n^{NN}(\mathbf{k}_{rel}, \mathbf{K}_{CM})$ are: i) at $K_{CM} = 0$, *i.e.* for nucleons moving exactly back-to-back, in the so-called correlated region $1.5 \text{ fm} \lesssim k_{rel} \lesssim 3.0 \text{ fm}$, the distribution as a function of k_{rel} , $n^{NN}(k_{rel}, K_{CM} = 0)$, has a shape which is similar to deuteron's S wave, in the proton-proton pair case, and similar to the deuteron's D wave, in the proton-neutron pair case [1]; ii) the node in the S wave is partially filled increasing A from ${}^3\text{He}$ and ${}^4\text{He}$ to ${}^{12}\text{C}$ and ${}^{16}\text{O}$ [3, 7, 8, 22, 23]; iii) for non-zero values of K_{CM} , we find a decreasing high-momentum tail, with respect to the $K_{CM} = 0$ case [3, 7, 8, 22, 23]; iii) the high-momentum tail of the proton-neutron distribution can be checked against TNC model of Ref. [40], where the deuteron distribution was convoluted with a Gaussian center of mass dependence to obtain a model two-body momentum distribution: the comparison shows that up to moderate values of K_{CM} , the deuteron shape is reproduced by realistic calculations [3, 7, 8, 22, 23]; iv) in the region of small values of K_{CM} and $1.5 \text{ fm} \lesssim k_{rel} \lesssim 3.0 \text{ fm}$, the proton-neutron distributions at $K_{CM} > 0$ can be obtained from the one at $K_{CM} = 0$ scaled by a factor which is given by $n_{CM}^{pn}(K_{CM})$ of Eq. (8), and depends only on the modulus of K_{CM} [3] (*cfr.* Fig. 1); v) starting from ${}^4\text{He}$ the Gaussian approximation of Ref. [40] seems to be a good one, and the agreement with the Gaussian shape is better in larger nuclei [3]; vi) the comparison of $n^{NN}(\mathbf{k}_{rel}, \mathbf{K}_{CM} = 0)$ with the deuteron distribution is an approximate one: it was found that extracting from the total distribution the only contribution due to proton-neutron pairs in a spin 0 and isospin 1 state, which is possible in our formalism both in the light nuclei as well as in the medium-heavy nuclei case, the agreement becomes quantitative and the ratio of the nucleus to deuteron distribution is a constant in the correlation region [3]. Moreover, we recently extended our analysis to the one-body momentum

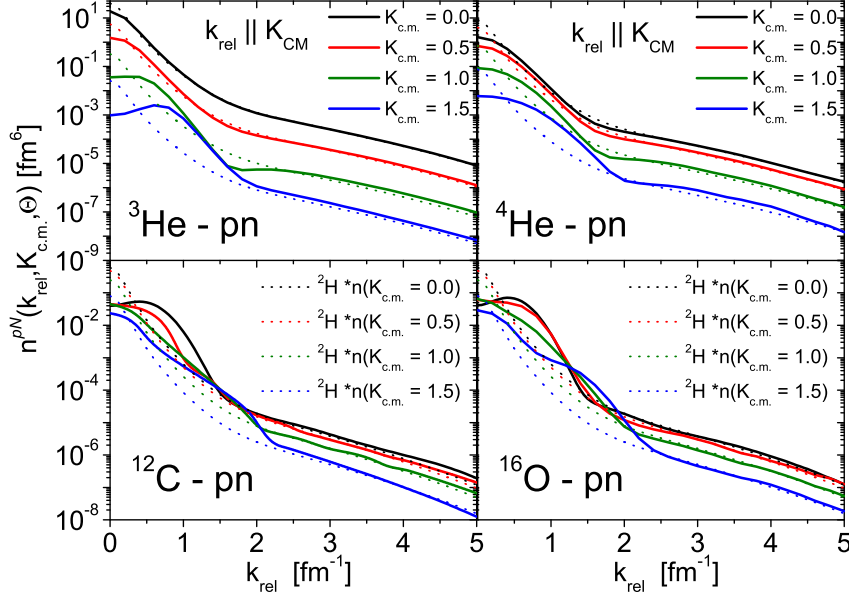


Figure 1. The relative two-body momentum distribution for a proton-neutron pair in ${}^3\text{He}$ and ${}^4\text{He}$ (top panels; after Ref. [3]) and in ${}^{12}\text{C}$ and ${}^{16}\text{O}$ (lower panels; after Refs. [22,23]) at fixed values $K_{CM}=0.0, 0.5, 1.0$ and 1.5 fm^{-1} of the center of mass of the pair. The various curves are compared to the deuteron distribution, multiplied by the value of $n(K_{CM}) = \int d\mathbf{k}_{rel} n(k_{rel}, \mathbf{K}_{cm})$ at the corresponding values of K_{CM} ; see Ref. [3] for details and additional calculations.

distributions case in great detail [6], showing that similar conclusions can be drawn as in the two-body distributions case, and that the TNC model of Ref. [40] can be effectively be updated exploiting the outcomes of the described realistic calculations, in view of the possible experimental measurement of correlated pairs in a nucleus in different spin and isospin states as well as carrying arbitrary center of mass momentum.

Such a detailed picture of SRC is experimentally limited to the ${}^{12}\text{C}$ nucleus, where one- and two-nucleon knockout were investigated in the correlation region, while correlations have been studied in a number of nuclei in inclusive electron scattering at $x = Q^2/2M_N\nu > 1$ and low ν . Experimental information on the center of mass momentum of a correlated pair in ${}^{12}\text{C}$ from Ref. [11] was compared with predictions made long before within the TNC model [41], finding quantitative agreement; nevertheless, as realistic calculations such as those presented in this report have become available for whole range of nuclei, it is now possible to go beyond the model predictions [3,6]. Additional experimental

information on the dependence of SRC on the center of mass of the pair and its isospin could be compared with theoretical calculations as the ones presented in this report. Our calculations of two-body distributions and their interpretation in terms of TNC model for correlated pairs allows one to single out the regions on the $\mathbf{k}_{rel}, \mathbf{K}_{CM}$ plane in which the various contributions to $n^{NN}(\mathbf{k}_{rel}, \mathbf{K}_{CM})$ are dominant. The region of small momenta is clearly dominated by the shell model contribution, while the region of high relative and small center of mass momenta of the pair is dominated by the two-nucleon correlations. As the center of mass momentum of the pair increase, configurations with three nucleons with vanishing total momentum start to dominate, and this is the region in which three-body correlations effects should be investigated, as it is argued in Ref. [3]. While experimental information on the relevance of three-nucleon correlations are still missing, evaluation of the contributions due to particular configurations of three nucleons whose total momentum is small seems to be feasible in the range of light to medium-heavy nuclei.

As we already mentioned, a full calculation of the processes used to directly observe SRC in ^{12}C is still missing. A consistent calculation should take into account the realistic initial state and full FSI between the knocked out nucleons and the residual nucleons, in the same way in which calculations for light nuclei has been performed (see [2, 42–47]) and have proven to reproduce cross section data. Inclusion of SRC in the initial state can be done by means of the notion of two-nucleon overlap function, the overlap between the initial A-body state and the (A-2)-body plus the two knocked out nucleons final state [48–53]. In particular, the approach of Ref. [51] where the authors perform calculations for two-proton knockout reactions with Jastrow correlations implemented with a linked cluster expansion similar to the one we used in our work, seems to be particularly suitable for an extension to realistically correlated wave functions calculated within our formalism. As a matter of fact, the Jastrow correlation functions misses the complexity of the full correlation structure induced by realistic potentials: in particular, they lack the tensor interaction which is a key ingredient for distinguishing basic properties of proton-proton as compared to proton-neutron correlations. For this reason an extension of the calculations of Ref. [51], in which only the reaction $^{16}\text{O}(e, e'pp)^{14}\text{C}(\text{g.s.})$ was discussed, with a fully correlated wave function, would be particularly meaningful. As far as FSI are concerned, it should be mentioned that the use of generalized Glauber multiple scattering approach for the rescattering of the knocked out nucleons in the final state in conjunction with realistic wave functions, in the case of light nuclei, proved to be very successful when comparing to experimental data, and basic features concerning the behavior of the correlated pair are reproduced by the TNC model. Calculations of distorted momentum distributions within the framework of the Glauber theory, and using correlated initial states for medium-heavy nuclei, can be performed in our formalism [26, 39, 54, 55] and suggest a common pattern across the range of nuclei we have investigated; partial results for complex nuclei, obtained with an extension the formalism of Ref. [26], are

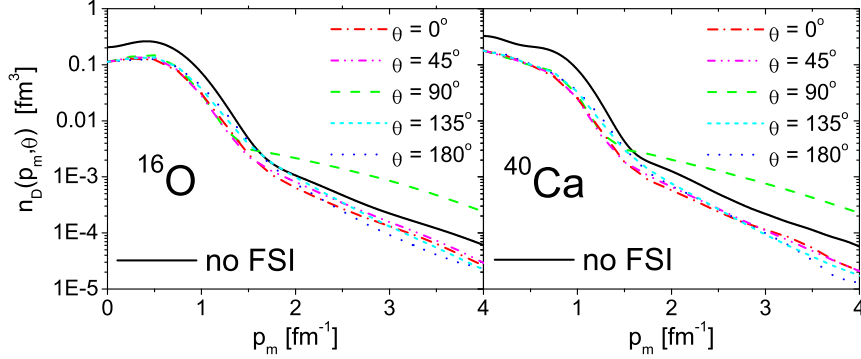


Figure 2. The distorted momentum distribution ^{16}O and ^{40}Ca calculated within the Glauber model for the FSI of the knocked out proton in an $A(e,e'p)X$ process and correlated nuclear wave functions, as proposed in Ref. [26].

shown in Fig. 2 (see [39]). The figure shows the quantity

$$n_D(p_m, \theta) = \frac{1}{(2\pi)^3} \int d\mathbf{r}_1 d\mathbf{r}'_1 e^{i\mathbf{p}_m \cdot (\mathbf{r}_1 - \mathbf{r}'_1)} \rho_D^{(1)}(\mathbf{r}_1; \mathbf{r}'_1). \quad (14)$$

The distorted momentum distribution of Eq. (14) correspond to a process $A(e,e'p)X$, with three-momentum transfer q and missing momentum \mathbf{p}_m ; θ is the angle between the missing momentum and the direction of propagation of the knocked out proton. This direction is singled out by the Glauber operator \hat{S} contained in the distorted density:

$$\rho_D^{(1)}(\mathbf{r}_1; \mathbf{r}'_1) = \sum_{\{\sigma, \tau\}} \int \prod_{j=2}^A d\mathbf{r}_j d\mathbf{r}'_j e^{i\mathbf{p}_m \cdot (\mathbf{r}_1 - \mathbf{r}'_1)} \Psi^*(\{\mathbf{x}\}) \hat{S}^\dagger \hat{\rho}^{(1)} \hat{S} \Psi(\{\mathbf{x}'\}), \quad (15)$$

and causes the original momentum distribution of the nucleon in the nucleus to be distorted and anisotropic, even if the target nucleus is a spherical one. As expected, the effect of FSI is different at the different values of the angle, and a similar pattern is exhibited by calculations at same angle in different nuclei, despite the different methods used to obtain the wave functions. A detailed comparison between the results for finite nuclei and the deuteron, and the extent to which similarities can be ascribed to universality of FSI within a correlated pair, is under investigation and will be reported in a separate publication.

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